

# A Profile Measurement System for Rail Quality Assessment during Manufacturing

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**Abstract**—Steel rails used in the transport sector and in industry are designed and manufactured to support high stress levels generated by high-speed and heavy-loaded modern trains. In the rail manufacturing process, one of the key stages is rolling, where fast, accurate and repeatable rail profile measurement is a major challenge. In this paper, a rail profile measurement system for rail rolling mills based on four conventional, inexpensive laser range finders is proposed. The range finders are calibrated using a common reference to properly express the point clouds generated by each range finder in the world coordinate system. The alignment of the point clouds to the rail model is performed by means of an efficient and robust registration method. Experiments carried out in a rail rolling mill demonstrate the accuracy and repeatability of the system; the maximum error is below 0.12%. All parallelizable tasks were designed and developed to be executed concurrently, achieving an acquisition rate of up to 210 fps.

**Keywords**—Industrial inspection; profile measurement; machine vision; range imaging; camera calibration.

## I. INTRODUCTION

Steel rails are used in the transport sector as well as in a wide variety of industries. In these scenarios, the high speed and heavy loads of modern trains require rail tracks designed and manufactured to support high stress levels. In the manufacturing process, one of the key stages is rolling. At the end of this stage rails must be inspected to verify that they meet the dimensional quality standards required by the customer. Current high-quality standards define tight shape tolerances, which must be met while maintaining high productivity rates. Thus, modern rail mills cannot be conceived without a number of machine-vision-based systems for monitoring and controlling the rolling process. In recent decades this type of tasks has been automated [1] and a wide range of 3D techniques for imaging and visualization in industrial environments has been proposed [2]. The development of machine vision devices at decreased costs, their miniaturization and their integration in industrial processes have increased the use of 3D imaging systems in industry [3]. Rail rolling mills, as well as many other industries where meeting the current demand for high quality standards is essential, have benefited from the use of 3D imaging.

Usually, 3D data acquisition techniques are classified into contact and non-contact techniques. The former touch the surface of the object by means of a mechanical sensor, whereas the latter use non-contact devices based on magnetic, optical or acoustic principles. Non-contact techniques are commonly

divided into passive, which use environmental or ambient light to illuminate the scene, and active, which control the illumination of the scene by projecting light patterns onto it [4]. The most commonly used 3D imaging systems in industry are based on active techniques, especially when these systems are required to work in harsh environments where passive methods are negatively affected by ambient or surrounding light.

Rails are systematically inspected for surface defects and wear using non-destructive evaluation [5]. Rail inspection is carried out in the manufacturing process in the rolling mill for quality assessment and assurance. Furthermore, rails are inspected while the railway tracks are operated in order to detect defects due to surface cracks, plastic deformations and wear. Contact-based rail inspection systems can apply tactile techniques, using mechanical devices with several leverages, to indirectly observe the rail geometry. Some other contact-based systems measure vertical and horizontal accelerations using moving vehicles [6]. In the recent years, systems tend to use non-contact techniques, mainly based on automated visual inspection using structured light [7], [8], [9], [10], [11].

In this paper, a machine-vision-based, non-contact profile measurement system (PMS) of rails for rail rolling mills is presented [12]. This system provides in-process measurements of several dimensions of rails based on geometric parameters of the transverse sections, also called profiles, of these rails. The PMS is based on active range imaging, specifically on laser triangulation, using four coupled laser range finders, similar to those used in other applications in the metal industry [13]. Experiments carried out both in the lab and in a rail mill demonstrate that the PMS provides accurate and repeatable measurements. The presented system has three main contributions: 1) Accurate rail quality inspection in rolling mills using conventional and inexpensive machine vision components; 2) A robust and accurate calibration procedure; 3) An efficient and robust method to align point clouds obtained from multiple range finders to rail models.

The reminder of this paper is organized as follows: Section II presents the the proposed approach; Section III describes system calibration and assessment; Section IV discusses the results obtained in the experiments; and finally, Section V reports conclusions.

## II. PROPOSED APPROACH

Designing a dimensional inspection system for rail manufacturing involves many factors: measurement volume, reli-

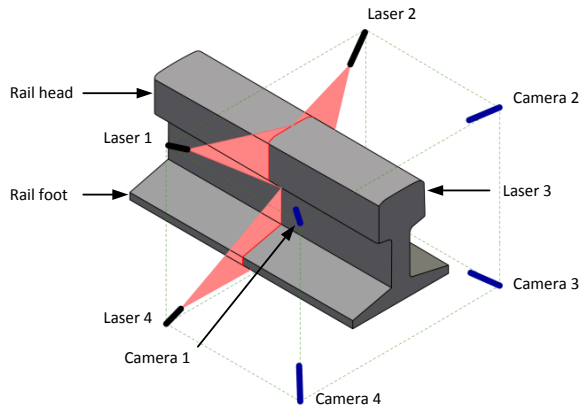


Fig. 1. Geometry of the proposed rail profile measurement system.

ability, accuracy, repeatability, cost, and computational speed, among others. Furthermore, the system may be constrained by environmental issues such as ambient light, temperature, humidity and dust. These factors and constraints are determinant in the geometry as well as the hardware and software components of the system.

#### A. Geometry

The rail PMS proposed in this paper uses four coupled laser range finders, as shown in Fig. 1 (laser emitter #3 is hidden because of the perspective). The location of the laser range finders is determined taking into account the dimensions of the rail head and foot (see Fig. 1), minimizing the occluded areas of the rail surface during the inspection process.

#### B. Active triangulation components

Each range finder is equipped with a CCD matrix camera: a DALSA Genie HM1400, featuring 1400x1024 pixel resolution. Each camera is equipped with a high-resolution, 16mm, Goyo GMTHR21614MCN lens. These cameras use a GigE Vision interface, a quad-port Intel Ethernet Server Adapter I350, connected to the host computer. On the other hand, each light pattern projected onto the rail surface is a single line generated by a Lasiris emitter with a diode power of 30 mW and a fan angle of 30°. Adjacent laser emitters project the laser pattern with different wavelengths, 660 nm and 685 nm. Thus, using an optical filter each camera is able to easily image the pattern projected by its counterpart emitter, mitigating the effect of the patterns generated by adjacent lasers.

#### C. Measurement pipeline

Fig. 2 depicts the five main stages of the PMS described in this paper: image acquisition, laser line detection and extraction, 2D to 3D coordinate translation, 3D rail profile computation, and dimensional measurement of the rail profile. The first three stages are replicated since they can run in parallel over independent data, following an MIMD approach. Each stage is a producer/consumer implemented following the pipeline pattern using parallel tasks and queues. Each task implements a stage of the pipeline, and the queues act as buffers that allow the stages of the pipeline to run concurrently, even though images are processed in order. Furthermore, if queues are sized properly, all tasks will meet the deadlines

imposed by the systems, even if any of them incur a time penalty due to exceptional circumstances. As can be seen, the first three tasks are divided in four sub-tasks, one per range finder, that can also run in parallel. Thus, all stages can run in parallel, and in three of them, data gathered from the four range finders are processed concurrently.

The measurement pipeline of the proposed system is implemented in a single process using C# and .NET Framework 4.0. Each element of the pipeline is implemented as a thread in the .NET thread pool: 14 threads implement the whole functionality of the measurement pipeline. Therefore, using a CPU with at least this number of cores ensures that all the elements of the pipeline can run in parallel. The last element of the pipeline, rail profile measurement, uses mathematical libraries programmed in C++, due to their performance. These libraries are wrapped into the C# project.

In this pipeline, the stages have unequal speeds. However, this is not a problem in the system since the most expensive stage is image acquisition (as will be shown in Section IV). Thus, given the fact that the first producer of the pipeline is the slowest one, the pipeline will never saturate.

#### D. Laser line detection and extraction

Laser line extraction is a straightforward task under controlled conditions of surrounding light and laser power [14]. However, common stripe extraction methods are highly sensitive to noise and they have major problems in industrial environments if they are not designed to deal with it correctly. In harsh environments a robust and accurate method capable of dealing with variable luminance, reflections which show up in images as noise, and uneven surfaces is required [15].

The PMS proposed in this paper extracts the single-line pattern projected onto the rail surface using a four-step procedure based on a well-known differential geometric algorithm [16]. In the first step, the image is smoothed by means of a convolution with a Gaussian kernel to yield good results detecting salient lines in the image. In the second step, the derivatives of the Gaussian kernel are used to determine a quadratic polynomial for each point of the image, which is used to calculate the line direction for each pixel based on the second derivative. In the third step, once individual line points have been extracted, they are linked into lines. This task is carried out based on an hysteresis threshold: points with a second derivative smaller than  $t_l$  are rejected; points with a second derivative larger than  $t_h$  are accepted; and the rest of the points are accepted if they are connected to accepted points by a connected path. In the last step, if more than one line was detected in previous steps, they are linked since gaps in the line are present in the image. The linking procedure is based on the regression lines of the extracted lines, where  $d$  is the maximum distance and  $\alpha$  is the maximum angle allowed for lines to be linked. Therefore, five parameters must be fine tuned for the laser line extractor to properly detect the lines in the image:  $\sigma$ ,  $t_l$ ,  $t_h$ ,  $d$ , and  $\alpha$ .

#### E. Rail profile computation

This is the first stage of the system where data provided by all range finders are synchronized (see Fig. 2), since the previous stages work as independent pipelines. In this stage

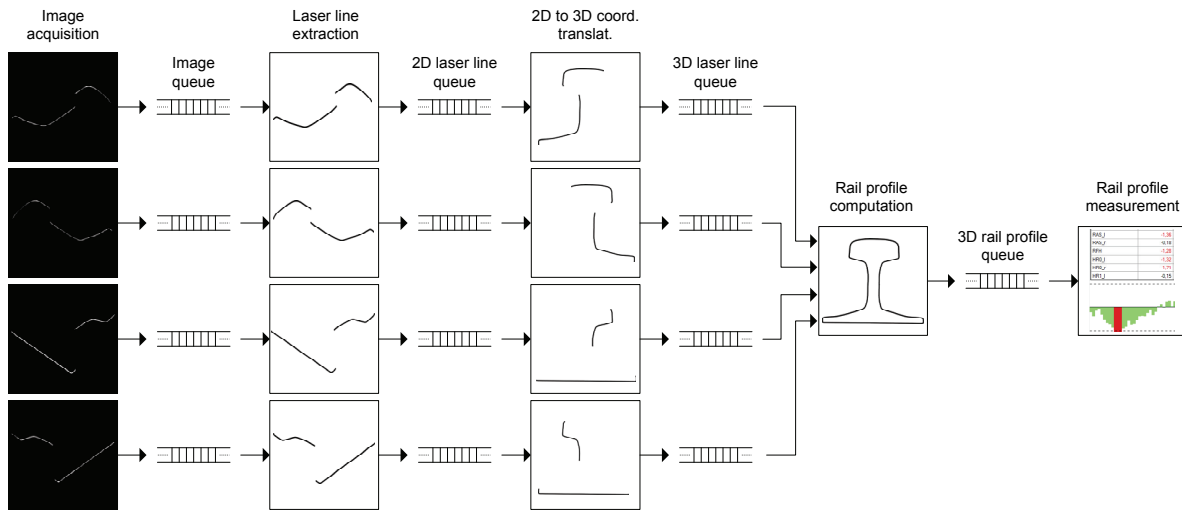


Fig. 2. Measurement pipeline of the proposed rail profile measurement system.

the partial rail contours generated by each range finder must be joined to create a rail profile at a specific Z coordinate of the rail track. Although the four pipelines connected to the four cameras of the system are identical, partial contours of the rail can reach this stage at slightly different speeds. Thus, a proper tagging and labelling method followed by a robust matching method are required to ensure that each partial contour is connected to other contours acquired at exactly the same Z coordinate of the rail track. Special attention must be paid if a frame is lost due to an external trigger failure, or if overflow in any queue of the pipeline is generated. These circumstances should never appear, but the proposed system is designed to automatically adapt to these issues, as described in [17].

Using the line extraction method described above, each range finder provides coordinates of the laser pattern projected onto the rail surface expressed in the coordinate system of its camera. In order to obtain metric measurements, points expressed in the coordinate system of the camera must be translated into the coordinate system of the world. Furthermore, since features extracted from several cameras are used to compute these measurements, a common reference system for all the range finders must be used. This reference system is computed in the second stage of the camera calibration procedure, i.e. in the calibration of extrinsic parameters, as will be described in Section III.

#### F. Rail profile measurement

The last stage of the pipeline provides metric measurements of the rail profile. It requires two steps. First, the rail data provided by the previous stage of the pipeline are aligned with a rail model. Second, the dimensions of the rail profile are computed. The output provided by the rail profile computation stage of the pipeline constitutes the data acquired from the rail profile expressed in the world coordinate system. This point cloud must be aligned with a rail model defined by the type of the rail-track that is being inspected. The alignment is performed by means of an efficient and robust registration method designed to accurately register 2D data to CAD models [18]. This method is an efficient variant of the ICP algorithm and aligns data obtained from standard structured light sensors

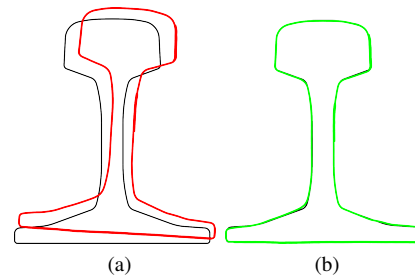


Fig. 3. Rail profile registration: (a) Point cloud and rail model; (b) Rail profile registered.

in less than one millisecond. It is based on geometric primitives on the 2D data rather than on points and uses a primitive caching method and an R-tree to accelerate the registration process. Fig. 3 shows the result of the registration process applied to the point cloud of a rail provided by the rail profile computation stage.

The rail primitives used in the registration process are listed in table I and are shown in Fig. 4 for both a symmetric and an asymmetric rail. These rail profile primitives are used to compute the rail profile dimensions listed in Table II. Fig. 5 shows several examples of rail profile dimensions computed using the rail profile primitives once the rail data has been registered to the rail model.

### III. CALIBRATION AND ASSESSMENT

The profile measurement system proposed in this work must compute metric measurements of the rail under inspection to check its dimensional quality. Thus, the system must be calibrated to get correspondences of the image pixels in the camera coordinate system (CCS), with the 3D coordinate system of the scene, that is, the world coordinate system (WCS).

#### A. Mathematical camera model

Camera calibration is the procedure that determines the parameters that model the optical projection of a point in the

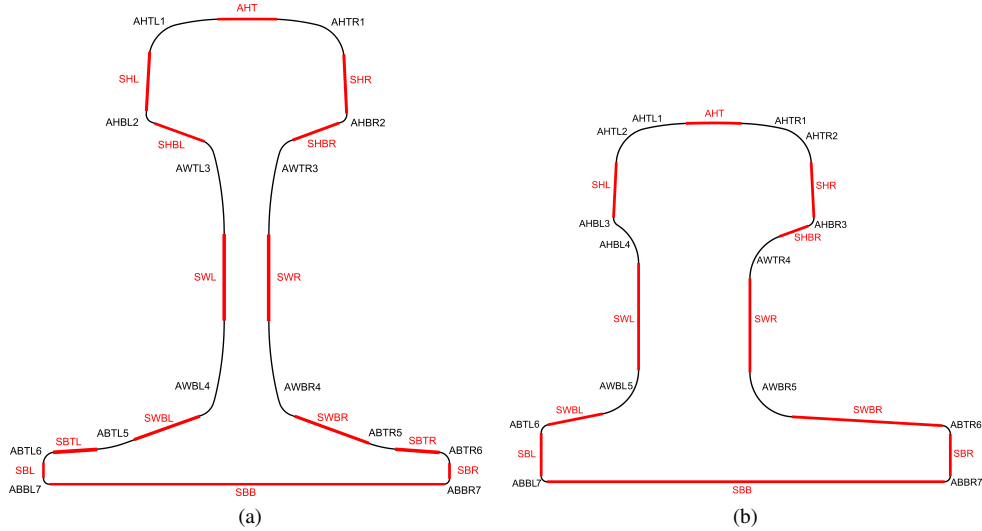


Fig. 4. Rail profile primitives: (a) Symmetric rail (rail model 60E1 in the standard UNE EN13674-1); (b) Asymmetric rail (rail model 54E1A1 in the standard UNE EN13674-1).

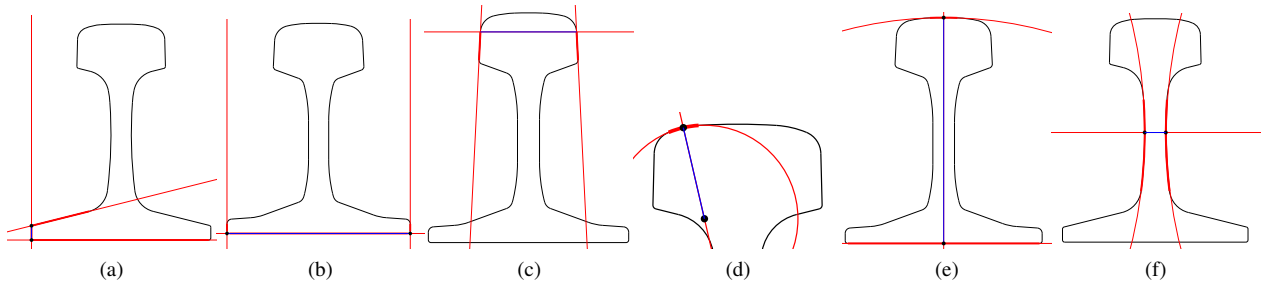


Fig. 5. Examples of rail dimensions computed using rail primitives. Thin red lines show segments and arcs fitting rail primitives; thick red lines show rail primitives; blue lines show computed rail dimensions: (a) Foot thickness left; (b) Foot width; (c) Head width; (d) Head radius; (e) Rail height; (f) Web thickness.

Primitive	Description
AHT	Arc Head Top
AHTL, AHTR	Arc Head Top Left/Right
SHL, SHR	Segment Head Left/Right
AHBL, AHBR	Arc Head Bottom Left/Right
SHBL, SHBR	Segment Head Bottom Left/Right
AWTL, AWTR	Arc Web Left/Right
SWL, SWR	Segment Web Left/Right
AWBL, AWBR	Arc Web Bottom Left/Right
SWBL, SWBR	Segment Web Bottom Left/Right
ABTL, ABTR	Arc Base Top Left/Right
SBTL, SBTR	Segment Bottom Top Left/Right
ABTL, ABTR	Arc Bottom Top Left/Right
SBL, SBR	Segment Bottom Left/Right
ABBL, ABBR	Arc Bottom Bottom Left/Right
SBB	Segment Bottom Bottom

Dimension	Description
RH	Rail Height
RFH	Rail Flange Height
FW	Foot Width
HF	Head Form
HW	Head Width
HWA	Head Width (Arema standard)
FT_l, FT_r	Foot Thickness left/right
RAS_l, RAS_r	Rail Asymmetry left/right
WT	Web Thickness
HR	Head Radius
FC	Foot Concavity

scene,  $P(x^w, y^w, z^w)$ , into a pixel (or a sub-pixel accuracy point) in the image,  $P'(r, c)$ , as shown in Fig. 6. The internal characteristics of the camera, such as sensor pixel size and lens distortions, are described by means of intrinsic parameters, whereas position and orientation of the camera are described by means of extrinsic parameters [19].

The calibration of the range finders that constitute the proposed PMS follows the non-linear camera model proposed

in [20], that maps 3D world coordinates  $(x_j^w, y_j^w, z_j^w)$  to pixel coordinates in the 2D camera sensor  $(r_j, c_j)$ , where  $j$  identifies the range finder ( $j \in [1, 4]$ ), by means of several transformations. The calibration procedure following this model is described in depth for a single laser range finder in [21].

Calibrating a 3D imaging system based on active triangulation using an area sensor involves computing the following three sets of parameters. The first comprises the intrinsic parameters of the camera model:  $\mathcal{I} = \{f, s^x, s^y, u_0, v_0, k_1, k_2, k_3, p_1, p_2\}$ , where  $f$  is the effective focal length;  $s^x$  and  $s^y$  are the image scale factors;

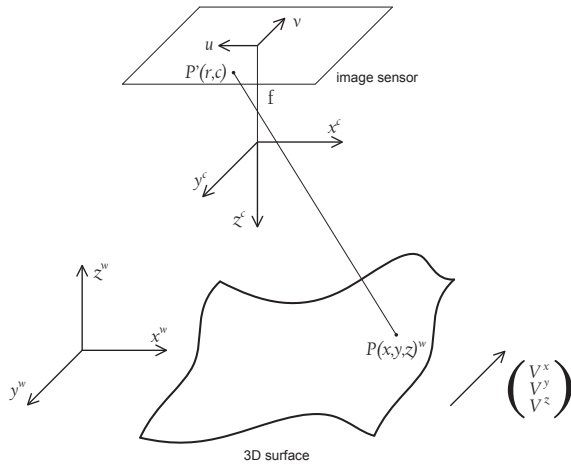


Fig. 6. Camera and perspective projection.

$u_0$  and  $v_0$  represent the principal point of the camera, also called the image center;  $k_1$ ,  $k_2$  and  $k_3$  are the coefficients for radial distortions; and  $p_1$  and  $p_2$  are coefficients for tangential distortions. The second comprises the extrinsic parameters of the camera model:  $\mathcal{E} = \{\alpha, \beta, \gamma, t_1, t_2, t_3\}$ , where  $\alpha$ ,  $\beta$  and  $\gamma$  are the Euler angles in the rotation matrix; and  $t_1$ ,  $t_2$  and  $t_3$  are the coefficients of the translation vector. The third set comprises the components of the motion vector of the object under inspection:  $\mathcal{V} = \{V^x, V^y, V^z\}$ .

The camera calibration procedure requires an array of precisely known 3D target points, or reference points,  $\{W = (X_i^W, Y_i^W, Z_i^W), i \in [1, n]\}$ , acquired from a calibrated pattern located in the scene. The 16 parameters of the mathematical model of each camera,  $\mathcal{M}_j = \{\mathcal{I}_j \cup \mathcal{E}_j\}, j \in [1, 4]$ , are estimated based on the array with corresponding feature points in the image sensor of the  $j$ -th camera,  $C_j = \{(X_i^{C_j}, Y_i^{C_j}), i \in [1, n], j \in [1, 4]\}$ . The estimation task relies on solving the non-linear least-squares problem shown in Eq.(1) for each range finder.

$$\min_{\mathcal{M}_j \in \mathbb{R}^{16}} \mathcal{F}_j(\mathcal{M}_j, C_j) = \sum_{i=1}^n ((x_{i,j}^c - r_{i,j})^2 + (y_{i,j}^c - c_{i,j})^2) \quad (1)$$

The calibration process of the proposed PMS involves calibrating four laser range finders. This process is similar to the calibration of a single range finder, but the calibration pattern must be in the field of view of all four cameras.

Once the mathematical camera model is solved, the transformation from 3D world coordinates to 2D image sensor coordinates can be carried out. The transformation from image coordinates to world coordinates is a simple procedure: the light plane, that is, the plane on which the single-line pattern fluctuates due to the shape of the product surface, is computed based on several images acquired with the calibrated pattern in the scene, one from each camera. Then the system is able to provide the 3D coordinates of a point in the scene based on a coordinate system fixed to this plane.

The length of the manufactured rail can be measured once the rail movement in the manufacturing line is calibrated. Since

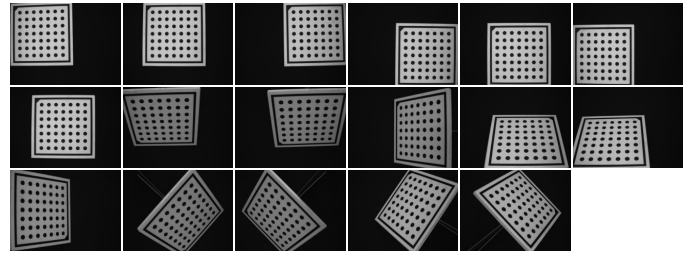


Fig. 7. Images for intrinsic parameter calibration.

the rail mill forces the rail to move along the longitudinal axis of the line,  $V^x$  and  $V^y$  will tend to be null. On the other hand,  $V^z$  will depend on the speed of the rail movement while manufacturing. Therefore, calibrating the speed of the rail movement requires calibrating the rotary encoder that supervises this movement.

### B. Calibration setup

The internal parameters and distortions of the camera are estimated by means of a planar-based calibration. A checkerboard pattern is imaged in several orientations and distances from the camera to identify a unique solution for  $\mathcal{I} = \{f, s^x, s^y, u_0, v_0, k_1, k_2, k_3, p_1, p_2\}$ . Fig. 7 shows the set of images acquired to estimate the internal parameters of a camera of the proposed PMS. The reference points are the centers of the circles printed in the pattern. The manufacturing procedure of the calibration plate guarantees that the locations of reference points have an error of less than  $50 \mu\text{m}$ , which gives an uncertainty of  $29 \mu\text{m}$ , computed as type B uncertainty evaluation [22].

The set of extrinsic parameters for each range finder is computed using a calibration pattern consisting of a flat aluminium surface with 13 protruding cylinders. The reference points are the center of each cylinder and its radius. Fig. 8a shows the calibration pattern illuminated by the laser emitters of the system in a laboratory setup. An example of images acquired by the four cameras of the system when the calibration pattern is illuminated by the laser line emitters can be seen in Fig. 8b This calibration pattern is also used in the rail mill for computing the extrinsic parameters of the camera models. The manufacturing procedure of the calibration object guarantees that the locations of the cylinders have an error of less than  $50 \mu\text{m}$ , which gives an uncertainty of  $29 \mu\text{m}$ , computed as type B uncertainty evaluation [22].

Laser lines are detected and extracted in the same way as described for the case of rail profile extraction (see section II-D). Fig. 8c shows the laser lines extracted from images in Fig. 8b. Said lines are then fitted to ellipses by the direct least square method. Ellipses are then filtered according to their likelihood to correspond to actual calibration cylinders, taking into account for each ellipse both its radius ratio and the length of the laser line in relationship with its shape. Ellipses that are rejected by either of these two filters are discarded. Then, an attempt is made to associate each of the ellipses that passed the filters with one of the calibration cylinders. This is done in four steps. In the first step, the centermost ellipse is found and associated with the centermost cylinder. In the second step, the coordinates of the ellipse centers are rotated by a predefined

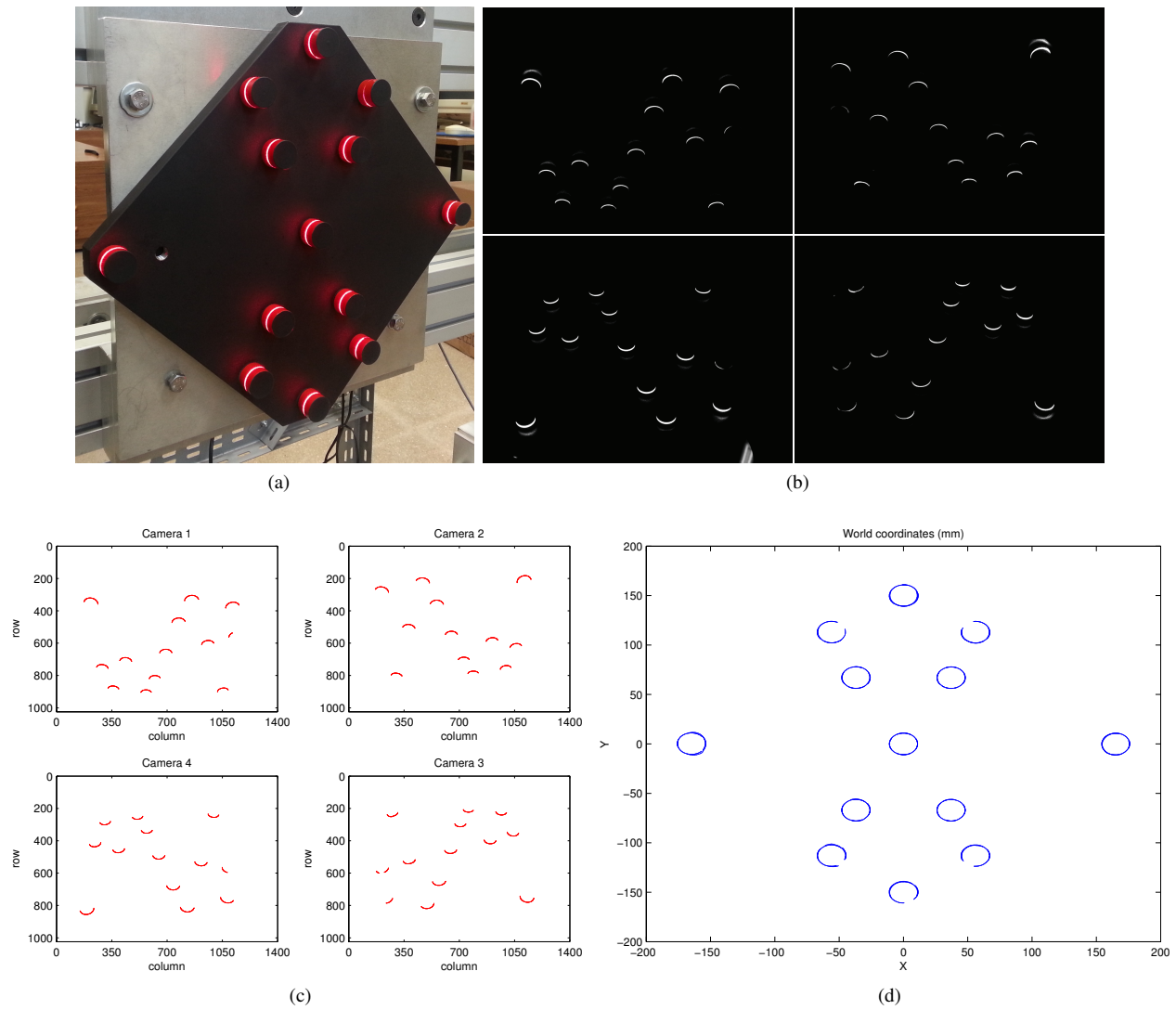


Fig. 8. Extrinsic parameter calibration: (a) Calibration pattern illuminated by the four laser line emitters of the system; (b) Calibration pattern imaged by the four cameras of the system (from top-left, clockwise: camera 1, camera 2, camera 3 and camera 4); (c) Laser lines extracted; (d) Features of the calibration pattern expressed in world coordinates.

amount in order to roughly compensate for the camera roll angle. In the third step, ellipse coordinates are constrained to the range  $[-1, 1]$  in such a way that the centermost point is assigned the coordinates  $(0, 0)$ , negative X coordinates are divided by the absolute value of the lowest (furthest from the center) negative X coordinate, positive X coordinates are divided by the value of the highest positive X coordinate and so on. Actual cylinder coordinates are constrained in the same way. In the fourth step, the coordinates of the ellipses are compared to those of the cylinders, and each ellipse is associated with the cylinder which is closest in Euclidean distance, unless another ellipse is closer to the same cylinder, in which case the first one is discarded. Ellipses whose distance to the cylinders is greater than an imposed threshold,  $t_{ec}$ , are also discarded. Correspondences between the (original, unconstrained) center coordinates of the remaining ellipses and the coordinates of their associated cylinders are then used to compute a pose. Fig. 8d shows the laser lines extracted by the four range finders and expressed in the WCS using the

calibration data computed as described above.

Before acquiring images with the calibration pattern in the scene the system must be set up to properly extract the single-line pattern from the acquired images. Thus, system calibration depends on parameter selection in the set-up process. In order to choose the best suited set of parameters, a factorial experiment was carried out. Different values for the acquisition time, the standard deviation of the Gaussian for the smoothing kernel, the distance limit for cylinder matching and the maximum number of ellipses to use in the pose computation, along with multiple variations of the direct least square method for ellipse fitting, were considered. Based on this experiment, two main parameters are identified as the main influence in the laser line extraction from the calibration pattern: the acquisition time,  $t$ , and the standard deviation of the Gaussian for the smoothing kernel,  $\sigma$ .

### C. Calibration assessment

In order to evaluate the accuracy of the camera calibration procedure described above, reprojection errors and the estimated focal length are shown to assess the calibration of internal parameters, and three different metrics computed over the calibration template are provided to assess the calibration of external parameters.

In the process used to obtain the internal parameters, the radial lens distortions was modelled using two models: analytical and numerical. The former uses only one parameter to model radial distortions,  $\kappa$ , whereas the latter is more complex and uses three parameters,  $k_1, k_2, k_3$ , as described in Section III-A. Although the accuracy achieved with the former is lower, it can be inverted analytically whereas the latter can only be solved numerically. Table III shows the reprojection errors for each camera of the system computed using these two models. The reprojection error expresses the average distance, in pixels, between the backprojected reference points of the calibration pattern and their extracted coordinates in the image plane. As can be seen, the largest reprojection error computed using a numerical model it is 0.16 pixels, whereas using an analytical model is below 0.17 pixels. In both cases, this ensures that the calibration process was successful. Although there is only a slight difference between the results of the two models, the calibration parameters obtained by the numerical will be used in the system. In addition, the estimated focal length of the lens of each camera is computed and shown in the table (the nominal focal length of each lens is 16 mm; see section II-B).

TABLE III. CALIBRATION ASSESSMENT: INTERNAL PARAMETERS

Camera	Distortion model	Reprojection error (pixels)	Focal length (mm)
Camera #1	Analytical	0.154	16.268
	Numerical	0.141	16.269
Camera #2	Analytical	0.164	16.225
	Numerical	0.154	16.231
Camera #3	Analytical	0.166	16.082
	Numerical	0.160	16.082
Camera #4	Analytical	0.169	16.143
	Numerical	0.163	16.144

Three different metrics were designed to assess the computation of external parameters: center distance (CD), radius difference (RD), and point distance (PD). The CD metric expresses the distance between the center of each cylinder in the calibration template and the center of each cylinder computed based on the image acquired by each laser range finder. The RD metric expresses the difference between the radius of each cylinder in the calibration template and the radius computed by the system based on images acquired by each range finder. The PD metric expresses the difference between the radius of each cylinder and the distance from the computed center of the cylinder to each of the sampled points of the cylinder. Table IV shows the errors of the external calibration of each range finder.

## IV. EXPERIMENTAL RESULTS AND DISCUSSION

The accuracy evaluation of rail profile measurements provided by the proposed PMS was examined using a prototype first in the laboratory and then in a rail rolling mill courtesy of ArcelorMittal Asturias. A randomly selected rail was inspected

TABLE IV. CALIBRATION ASSESSMENT: EXTERNAL PARAMETERS (UNITS IN MM)

Camera	CD			RD			PD		
	mean	STD	max.	mean	STD	max.	mean	STD	max
Camera #1	0.176	0.035	0.221	0.101	0.038	0.158	0.097	0.015	0.116
Camera #2	0.159	0.058	0.271	0.076	0.053	0.194	0.123	0.034	0.180
Camera #3	0.299	0.031	0.343	0.047	0.019	0.065	0.226	0.040	0.297
Camera #4	0.185	0.069	0.274	0.169	0.049	0.250	0.106	0.035	0.175

TABLE V. ACCURACY OF DIMENSIONAL INSPECTION (UNITS IN MM)

Dim.	Length	PMS-GT					MP-GT
		#1	#2	#3	#4	#5	
HW	10000	-0.02	-0.04	-0.06	-0.04	-0.04	0.15
FW	10000	0.01	-0.01	-0.03	-0.02	-0.03	-
RH	10000	-0.08	-0.10	-0.09	-0.11	-0.11	-
HW	20000	0.05	0.04	0.04	0.04	0.03	0.15
FW	20000	0.03	0.02	0.03	0.03	0.03	-
RH	20000	-0.16	-0.16	-0.12	-0.12	-0.12	-
HW	30000	0.03	0.03	0.03	0.04	0.01	0.07
FW	30000	-0.05	-0.04	-0.06	-0.05	-0.05	-
RH	30000	-0.15	-0.19	-0.14	-0.14	-0.17	-
HW	40000	0.01	0.01	0.01	0.00	0.01	0.05
FW	40000	0.00	0.04	0.00	0.02	0.01	-
RH	40000	-0.19	-0.19	-0.20	-0.19	-0.19	-
HW	50000	-0.01	0.00	0.00	0.01	0.00	0.08
FW	50000	0.03	0.03	0.02	-0.01	0.00	-
RH	50000	-0.19	-0.19	-0.20	-0.20	-0.19	-
HW	60000	0.00	0.00	0.00	-0.01	0.00	0.13
FW	60000	0.01	-0.01	-0.02	-0.01	-0.03	-
RH	60000	-0.13	-0.12	-0.11	-0.12	-0.07	-

five consecutive times under the same working conditions. The model of the rail is 60E1, according to the standard UNE EN13674-1. This rail track was also inspected in the rail rolling mill with a Greenwood MiniProf Rail gauge<sup>1</sup> featuring an accuracy better than  $\pm 11 \mu\text{m}$  and a repeatability of  $\pm 2.5 \mu\text{m}$ . Once the rail was inspected in the mill, it was cut into pieces, and several specimens were measured in the metrology lab of the R&D Centre of ArcelorMittal in Asturias using a Trimos Temp 1282 coordinate-measuring machine (CMM) featuring an accuracy better than  $\pm 1 \mu\text{m}$  in FW and better than  $\pm 20 \mu\text{m}$  in HW and RH. Dimensions provided by the MiniProf gauge and the CMM are used to assess the dimensions computed by the PMS.

Table V shows differences among the measurements computed by the dimensional inspection system proposed in this paper, PMS (five repetitions of the experiment), and the measurements carried out by the technicians in the metrology lab, considered the ground truth, GT. Also, differences with the dimension provided by the MiniProf Rail gauge, MP, are shown. As can be seen, errors provided by the system are between  $-0.05 \text{ mm}$  and  $0.20 \text{ mm}$ . This means that dimensions provided by the proposed PMS for HW, FW and RH have an error of less than  $0.12 \%$

In addition to accuracy, in order to evaluate the performance of the PMS, a repeatability evaluation is carried out to assess the consistency of the system. The repeatability evaluation expresses the range of measurements provided for the same dimension of the same rail specimen under consistent conditions. This test was carried out using the same method, on

<sup>1</sup><https://www.greenwood.dk/miniprofrail.php>

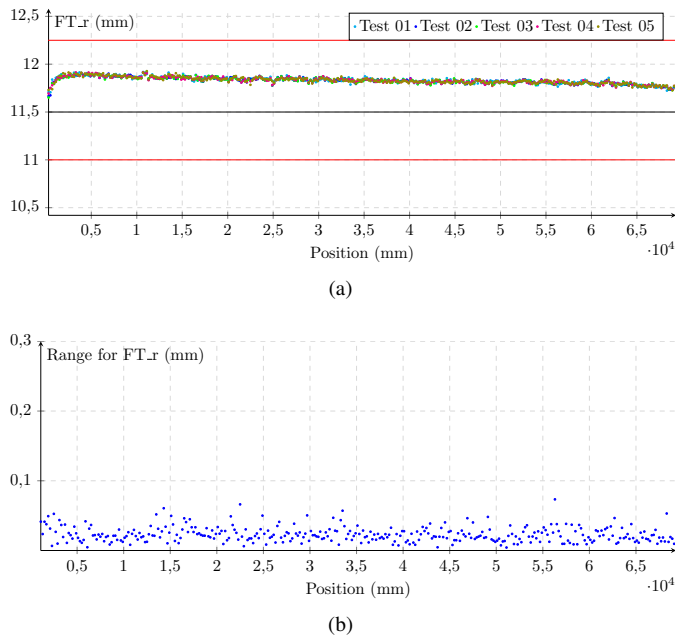


Fig. 9. Results of the repeatability evaluation for *Foot Thickness right* (FT<sub>r</sub>): (a) Computed values (the black horizontal line is the expected value, while the red horizontal lines are the maximum and minimum tolerated values); (b) Measurement range.

TABLE VI. REPEATABILITY OF DIMENSIONAL INSPECTION (UNITS IN MM)

Length	FC	FT_l	FT_r	FW	HW	HWA	RAS_l	RAS_r	RH	WT
10000	0.018	0.041	0.024	0.039	0.029	0.039	0.109	0.108	0.030	0.060
20000	0.013	0.046	0.026	0.035	0.021	0.016	0.099	0.108	0.038	0.071
30000	0.010	0.039	0.024	0.029	0.018	0.015	0.085	0.100	0.041	0.055
40000	0.012	0.037	0.023	0.032	0.018	0.014	0.098	0.105	0.025	0.048
50000	0.012	0.043	0.022	0.036	0.020	0.014	0.095	0.108	0.015	0.065
60000	0.016	0.049	0.022	0.031	0.021	0.017	0.084	0.096	0.032	0.049

the same item, in the same installation, by the same operator and using the same system within short intervals of time, according to ISO 5725-1:1994. Fig. 9 shows an example of the repeatability evaluation. Fig. 9(a) shows the computed values for the five consecutive inspections of the rail for FT<sub>r</sub>, and Fig. 9(b) shows the range of the measurements for this dimension in the five runs. Red lines indicate the lower and upper limit imposed by the specification to which the rail is manufactured; the black line is the expected value according to the specification. Table VI shows the range of all the dimensions computed by the system, expressed as the average of the ranges each 10 m of the rail. As can be seen, the system is highly repeatable.

Finally, the running time of the system is analysed. The host computer used by the PMS is an HP Z620 Workstation equipped with an Intel Xeon E5-2643 v2 processor (6 cores @ 3.5 GHz) and 12 GB of RAM memory. The elapsed time in each stage of the pipeline was measured in ten consecutive rails inspected in the rail mill. Table VII shows the computing times: mean, standard deviation (SD) and the upper limit of the 99% confidence interval (UCL). Taking this information into account, the system is able to work with an acquisition rate up to 210 fps. In the aforementioned experiments the acquisition time of the cameras was set to 15 ms after several experiments with different surface conditions of rails and lens apertures.

Thus, the acquisition rate was limited to 66 fps.

TABLE VII. RUNNING TIMES (UNITS IN MS)

	Laser line extraction	2D to 3D translation	Rail profile computation	Rail profile measurement
mean	4.62	0.01	0.02	3.09
SD	0.44	<0.01	<0.01	1.72
99% UCL	4.68	0.01	0.03	3.16

## V. CONCLUSIONS

In modern rail rolling mills, accurate and repeatable profile measurements are crucial for inspecting and assessing rails that will be used in the transport sector by high-speed trains and in industry by heavy-loaded trains. The system proposed in this paper uses four conventional, inexpensive laser range finders to measure transverse sections of rails. The range finders are calibrated following a non-linear camera model using a common reference to properly express the point clouds in the world coordinate system. Then point clouds are aligned to the rail model by means of an efficient and robust registration method.

The experiments carried out in the laboratory and in a rail rolling mill demonstrate the accuracy and repeatability of the system. Depending on the dimension, errors provided by the system are between  $-0.05$  mm and  $0.20$  mm, with a maximum error of less than  $0.12\%$ . Furthermore, all parallelizable tasks were designed and developed to be executed concurrently. Thus, the proposed rail profile measurement system is able to work with an acquisition rate of up to 210 fps, that allows capturing high density 3D data of the rail.

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