

Research Article

Low-Cost Monitoring System of Sensors for Evaluating Dynamic Solicitations of Semitrailer Structure

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Analysis of the fatigue life of a semitrailer structure necessitates identification of the loads and dynamic solicitations in the structure. These forces can be introduced in computer simulation software (multibody + finite element) for analysing the response of different design solutions to them. These numerical models must be validated and some parameters need to be measured directly in a field test with real vehicles under various driving conditions. In this study, a low-cost monitoring system is developed for application to a real fleet of semitrailers. According to the definition of the numerical model, the guidance of a virtual vehicle is defined by the three-dimensional kinematics of the kingpin. For characterisation of these movements, a monitoring system having a low-cost inertial measurement unit (IMU) and global positioning system (GPS) antennas is developed with different configurations to enable analysis of the best cost-benefit (result accuracy) solution, and an extended Kalman filter (EKF) that characterises the kinematic guidance of the kingpin is proposed. A semitrailer was equipped with the experimental low-cost monitoring system and high-precision sensors (IMU, GPS) in order to validate the results obtained by the experimental low-cost monitoring system and the inertial-extended Kalman filter developed. The validated system has applicability in the low-cost monitoring of a fleet of real vehicles.

1. Introduction

Vehicle weight reduction is one of the effective approaches for reducing fuel consumption and emissions [1]. A simulation has revealed that, for every 10% weight reduction from the weights of an average new car and light truck, their fuel consumption would reduce by 6.9% and 7.6%, respectively. In the case of a commercial vehicle, a reduction in its kerb weight corresponds to an increased payload capacity. Therefore, weight reduction has a greater impact for this type of vehicle than for other types of vehicles.

In semitrailers, the body frame represents more than 75% of the total weight; therefore, this component has the most room for improvement. Weight reduction of the body frame should be achieved while keeping the safety level of the

vehicle and the ability of the vehicle and of its components to maintain their functions unchanged or while limiting the vehicle's degradation with aging to acceptable levels.

Today, for heavy-duty trucks, an adequate endurance specification is assumed when 10% of the population of vehicles produced exceed the 800,000 km without any failure [2]. Phenomena that can influence the endurance of a vehicle can be classified into the following categories: fatigue, wear, corrosion, and shocks and collisions.

Weight reduction of the body frame of a vehicle affects its fatigue life; therefore, to ensure that the aging and endurance remain unaffected by this reduction, it is necessary to establish the vehicle design on the basis of a detailed study of the fatigue life. Fatigue life evaluation necessitates an accurate identification of the loads that the body frame

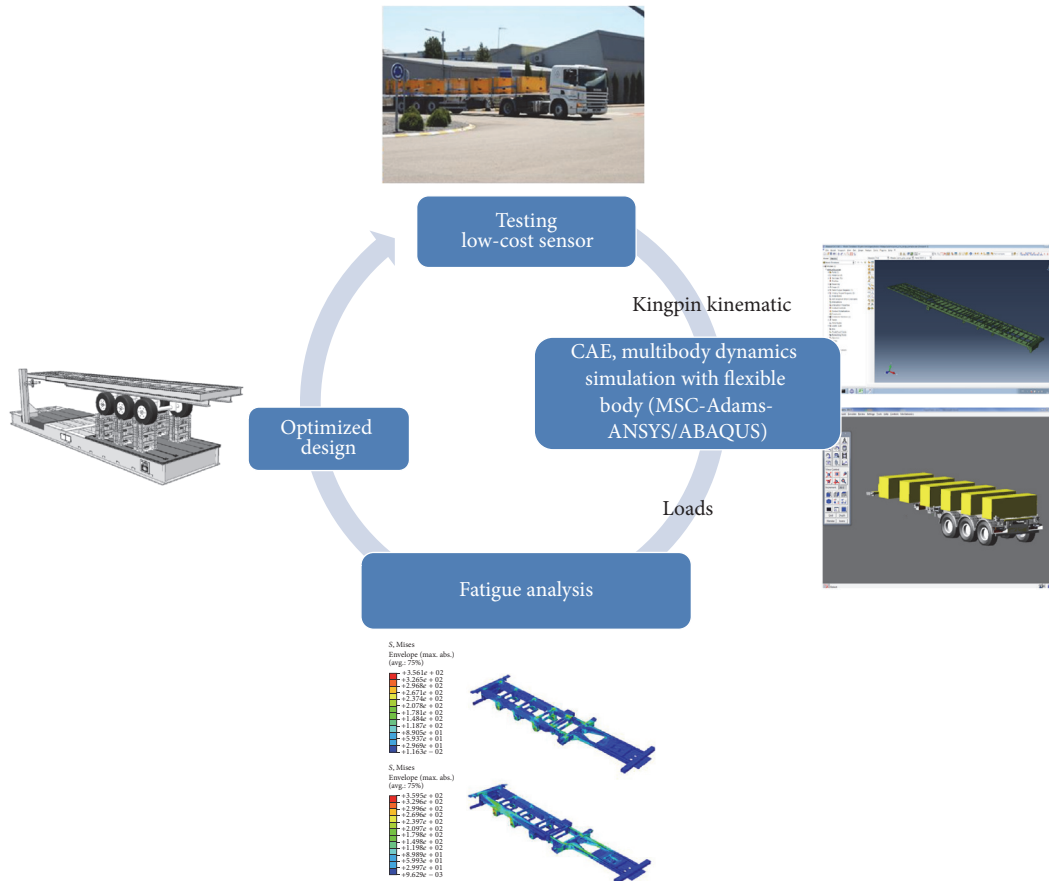


FIGURE 1: Methodology for fatigue life calculation.

will be subjected to during operation and performance of optimization by the use of simulation techniques based on the Finite Element Method. The methodology for fatigue life calculation is established by means of a virtual test, as shown in Figure 1.

As shown in this figure, a real vehicle is employed for performing discretisation of the body frame by means of finite element software (such as ANSYS or ABAQUS). This chassis information is then introduced in multibody dynamics simulation software (such as ADAMS of MSC Software Co.) to develop a virtual experimental program. This program includes different driving conditions (speed, manoeuvres, obstacles, roads, etc.) with the aim of defining the load cases to be introduced in fatigue life prediction algorithms.

To determine the loads during vehicle operation, a methodology based on the simulation of virtual models using data acquired by low-cost instrumentation has been developed. The effectiveness of this methodology—which combines acquired real data and a virtual model to optimise designs—for application to other types of vehicles has been proved [3]. The main advantage of combining a virtual model and real data is the reduction in the complexity of the data acquisition system and the required number of sensors. In a vehicle such as that analysed, the loads necessary for

calculation of the fatigue life are due to the actions of tractor, suspension, load, and so forth [4, 5]. This implies the need for complex instrumentation, thereby making this methodology unsuitable for application to a vehicle fleet.

The present paper presents the development and implementation of a low-cost instrumentation system that is nonintrusive and robust; this system was developed with the aim of applying the above-described methodology to trailer-type vehicles. A semitrailer is a vehicle that can be coupled to different tractor vehicles. Therefore, in order for the virtual model to be able to calculate the loads regardless of which tractor vehicle is connected to the semitrailer, the inputs to the virtual model are proposed to be the actions of the tractor vehicle at the point of connection.

The multibody model inputs developed for use with the methodology can be forces, acceleration, velocities, and/or positions. Given the need to develop a low-cost system to provide inputs to the model, the kinematic guidance of the connection point (i.e., kingpin) between the tractor and the semitrailer was selected as the input in the present study.

2. Materials and Methods

2.1. Related Work. The most appropriate device for measuring the velocity of the kingpin is a Global Navigation

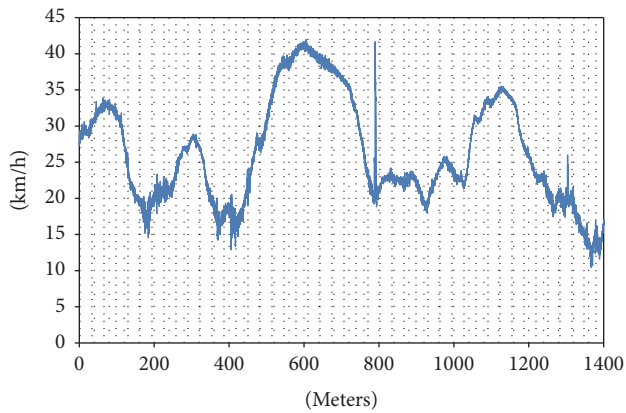


FIGURE 2: Variations in measured velocity due to noise in GNSS in actual test.

Satellite System (GNSS) receiver, because two of the outputs are the absolute speed and the course angle (as of April 2013, only the United States NAVSTAR global positioning system (GPS) and the Russian GLONASS were global operational GNSSs). However, the velocity acquired with a low-cost GNSS receiver causes two problems—a high level of noise and low precision, which worsen under the influence of external factors such as multipath and low satellite visibility [8]. Given the environment in which these vehicles operate, these problems occur frequently. Noise in the GNSS signal implies variations in the measured velocity, which in turn implies significant changes in acceleration (Figure 2). During simulation, these variations in the input of the virtual model translate into loads much higher than actual loads. Fatigue analysis based on thus obtained loads would be unreliable, and filtering of the input signal would not solve this problem. Furthermore, speed measurement of the kingpin using a GNSS receiver cannot be performed for all types of vehicles, since the kingpin is usually hidden under the box or the load, and this approach is applicable only in the case of a semitrailer or container.

In consideration of both of these problems, the low-cost system developed in the present study is equipped with an inertial filter—specifically, an inertial-extended Kalman filter (i-EKF)—for the estimation of velocity of the kingpin using a GNSS receiver, which can be placed at a different location. The proposed low-cost system is based on the concept of fusion of an inertial measurement unit (IMU) and GNSS receivers with low-cost sensors. Sensor fusion refers to the combination of data acquired from multiple sensors with related information, which facilitates achievement of more specific inferences than those possible by using a single independent sensor [9]. The following are the advantages of using a multisensor approach over a single-sensor approach [10]:

- (i) Robust operational performance: any of the sensors has the potential to provide information during unavailability malfunctioning or failure of the other sensors.

- (ii) Extended temporal coverage: one sensor is able to detect or measure an event at times when the other sensors are unable to.
- (iii) Extended spatial coverage: one sensor can cover what other sensors cannot.
- (iv) Increased confidence: multiple independent measurements provide information on the same event.
- (v) Improved detection performance: multiple independent measurements of the same event are integrated effectively.
- (vi) Reduced vulnerability to denial: this occurs as a result of increased dimensionality of the measurement space.

The following are the advantages of sensor-fused data over single-sensor data [9]:

- (i) Improved estimate: if several identical sensors are used, combination of observations from these sensors may lead to an improved estimate. Furthermore, a statistical advantage is gained by the addition of independent observations, under the assumption that the data are combined in an optimal manner.
- (ii) Improved observation process: use of the relative placement or motion of multiple sensors may result in an improved observation process. For example, two sensors that measure the angular directions to an object can be coordinated to determine the position of the object via triangulation.
- (iii) Improved observability: broadening of the baseline of physical observables can result in significant improvements. If the observations are associated correctly, the combination of sensors provides a better estimation than what could be obtained by any of the sensors independently. This results in a smaller error region.

The fusion of an IMU and GNSS receiver is frequently used for accurate determination of attitude. In [11], with the aim of determining the full attitude even for a nonaccelerating vehicle, a navigation system that incorporates inertial and two-antenna carrier phase differential GPS measurements was developed. Aided inertial navigation is a well-studied problem [12–16]. Several GPS pseudorange and Doppler-aided inertial systems have been documented in the literature; see, for example, [17].

A low-cost system that fuses inertial sensing and a two-antenna GPS with an unscented Kalman filter (UKF) has been developed in [18]. Many previous works on low-cost attitude estimation [19–28] have focused on the fusion of inexpensive sensors, including microelectromechanical system-(MEMS-) based gyroscopes and accelerometers, magnetometers, and the GPS.

In low-cost land vehicle navigation applications, in addition to accurate position and velocity information being required, an accurate attitude needs to be provided by the navigation system [28–31]. Use of the GPS signal for attitude determination has several advantages such as the small size, low cost, lack of cumulative errors, and high accuracy of

the GPS. However, attitude determination using the GPS also has drawbacks such as its susceptibility to the external environment and instability in dynamic applications [31]. The conventional method of attitude determination is to use an inertial navigation system (INS). However, the INS has a drawback in that errors accumulate over time, especially in the case of a low-cost MEMS-INS. If the GPS and MEMS-INS are combined effectively, the reliability and accuracy of attitude determination can be improved [32–34].

The low-cost system proposed in this work differs from conventional systems in that it entails estimation of the velocities (to be used as inputs in computer simulation models) at a point of the vehicle and not the position or attitude. In any case, given the advantages of the fusion of these sensors, estimation of other states that are inputs to safety systems is a routine methodology for a vehicle.

Several works have proposed estimation methods of several key vehicle states—sideslip angle, longitudinal velocity, roll, and grade—for example, by combining automotive-grade inertial sensors with a GPS receiver [35]. Kinematic estimators that are independent of uncertain vehicle parameters integrate inertial sensors with GPS antennas to provide high update estimates of the vehicle states and sensor biases. Use of a two-antenna GPS system would enable quantification of the effects of pitch and roll on the measurements, which have been demonstrated to be quite significant in sideslip angle estimation.

The sideslip angle is an important state of vehicle lateral dynamics, and its estimation has been studied by many researchers [36–45]. For example, Bevly et al. proposed an estimation method that utilises a single-antenna GPS along with an IMU [43, 44]. This method essentially integrates the bias-corrected yaw rate to obtain the vehicle heading angle, which can provide the sideslip angle along with the vehicle velocity angle measured by the single-antenna GPS. In [46], a new method was proposed that employs two low-cost single-antenna GPS receivers to estimate the vehicle sideslip angle. In the present study, four kinematics equations that relate the velocities of two different GPS receivers to the heading angle and to the longitudinal/lateral velocities of a vehicle are presented. These equations are then analysed in order to determine the theoretical limit of the sideslip/heading angle estimation. Fusion of a GPS with an IMU through an EKF is performed.

2.2. Mathematical Model. A mathematical model of a semi-trailer is established in this section. This model is then used in a computer simulation to implement an EKF with a low-cost IMU and GPS receivers. According to the definition of the mathematical model, the longitudinal and lateral acceleration values (vehicle frame) and the yaw rate provided by the IMU are used as inputs. The GPS speed (reference frame) is considered as an output or measurement vector.

2.2.1. Reference and Vehicle Frames. For the definition of the vehicle dynamics model and computer simulation model, the kinematics of the kingpin should be defined as an input by characterising its speed. According to the usual approach

of using a multibody system, it is necessary to define the kinematics in local coordinates in accord with the motion of the vehicle. Given that the employed sensing system includes various types of sensors, two reference systems are defined.

Reference Frame. The following is the notation of coordinates used for the reference frame (sometimes termed the local vertical, local horizontal (LVLH) frame): east, north, up (ENU). The local ENU coordinates are formed from a plane tangential to the Earth's surface, fixed at a specific location; therefore, this plane is sometimes known as a “local tangent” or “local geodetic” plane.

Vehicle Frame. In this case, the sensitive axes of the accelerometer sensor are made to coincide with the axes of the semitrailer. The origin coincides with the location of the kingpin of the vehicle.

This frame is in accordance with the ISO standards, specifically ISO 8855. In this coordinate system (Figure 3), the forward movement of the vehicle is described along the positive x -axis; the lateral movement of the vehicle is described along the y -axis; it is positive when the vehicle is oriented to the left (from the driver's position); and the vertical movement of the vehicle is described along the z -axis.

2.2.2. Extended Kalman Filter. In order to apply the proposed methodology, the equations of the virtual model must be expressed in space-state form. The state-space representation of a physical system is composed of a set of inputs, outputs, and state variables related via first-order differential equations, which are combined in a first-order matrix differential equation. The state variables or states are expressed as vectors and the algebraic equations are written in matrix form, provided that it is a linear system. A general way to represent a nonlinear system with p inputs, q outputs, and n states is as follows:

$$\begin{aligned}\dot{x}(t) &= \mathbf{f}(t, x(t), u(t), w(t)), \\ y(t) &= \mathbf{h}(t, x(t), u(t), v(t)).\end{aligned}\tag{1}$$

Here, the first equation is the state equation and the second one is the output equation, where $x(t)$ is the “state vector,” $x(t) \in \mathbb{R}^3$; $u(t)$ is the “input vector,” $u(t) \in \mathbb{R}^3$; $y(t)$ is the “output vector,” $y(t) \in \mathbb{R}^q$; and $w(t)$ and $v(t)$ are random variables that represent the process noise and measurement noise, respectively.

Applying the concept of Taylor series expansion, the estimation around the current estimate can be linearised using the partial derivatives of the process and the measurement functions in order to compute estimates even in the face of nonlinear relationships. It can be assumed that the system has a state vector $x(t) \in \mathbb{R}^n$ and that it is governed by the nonlinear stochastic difference equation. In discrete form, the equation can be expressed as

$$\begin{aligned}x(k) &= \mathbf{f}(x(k-1), u(k-1), w(k-1)), \\ y(k) &= \mathbf{h}(x(k), u(k), v(k)),\end{aligned}\tag{2}$$

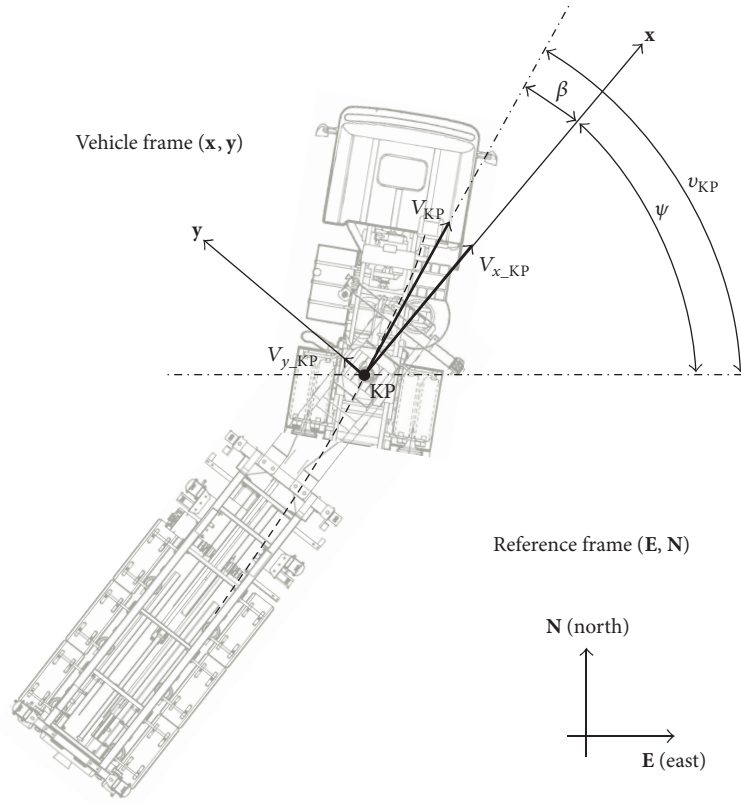


FIGURE 3: Reference and vehicle frames.

where the measurement equation is

$$y(k) = \mathbf{h}(x(k), u(k), v(k)). \quad (3)$$

In this case, the nonlinear function “ \mathbf{f} ” is the difference equation that relates the state at the previous time step ($k-1$) to that at the current time step (k). The state vector ($x(t) \in \mathbb{R}^3$) is defined as follows:

$$x(k) = \begin{bmatrix} x_1(k) \\ x_2(k) \\ x_3(k) \end{bmatrix} = \begin{bmatrix} V_{x_KP}(k) \\ V_{y_KP}(k) \\ \psi(k) \end{bmatrix}. \quad (4)$$

Further, $u(t) \in \mathbb{R}^3$, which represents the inputs from the IMU (acceleration and yaw rate), is expressed as

$$u(k) = \begin{bmatrix} u_1(k) \\ u_2(k) \\ u_3(k) \end{bmatrix} = \begin{bmatrix} a_{x_KP}(k) \\ a_{y_KP}(k) \\ \dot{\psi}(k) \end{bmatrix}. \quad (5)$$

$w(t)$, which represents the process and measurement noises, is given as

$$w(k) = \begin{bmatrix} w_1(k) \\ w_2(k) \\ w_3(k) \end{bmatrix} = \begin{bmatrix} \eta_{V_{x_KP}} \\ \eta_{V_{y_KP}} \\ \eta_{\psi} \end{bmatrix}. \quad (6)$$

Finally, $y(t)$ represents the “output vector” and $y(t) \in \mathbb{R}^q$. Its value is obtained via different study cases and it depends on the adopted instrumentation system and layout, as described later.

In practice, the individual values of the noises $w(k-1)$ and $v(k-1)$ at each time step are unknown. However, the state and measurement vectors without these values can be, respectively, approximated as

$$\begin{aligned} \tilde{x}(k) &= \mathbf{f}(\tilde{x}(k-1), u(k-1), 0), \\ \tilde{y}(k) &= \mathbf{h}(\tilde{x}(k), u(k), 0), \end{aligned} \quad (7)$$

where $\tilde{x}(k)$ is some *a posteriori* estimate of the state (from a previous time step k).

2.2.3. Development of the Mathematical Model of Semitrailer Using *i*-EKF. It is considered that the vehicle (semitrailer) performs a flat movement and that it is guided by the tractor unit (truck), as described in Figure 3. The implemented vehicular dynamics model takes into account the inertial effects, but it does not consider dynamic roll, suspension performance, inclination of the road, and so forth. For the formulation of the system dynamics model in the state-space form, the acceleration in the mobile system of the kingpin is

considered; accordingly, the model can be expressed in terms of linear and angular velocities as follows:

$$\begin{aligned} a_{x_KP} &= \dot{V}_{x_KP} - V_{y_KP} \cdot \dot{\psi}, \\ a_{y_KP} &= \dot{V}_{y_KP} + V_{x_KP} \cdot \dot{\psi}, \end{aligned} \quad (8)$$

where a_{x_KP} and a_{y_KP} are longitudinal and lateral acceleration, respectively, at the kingpin (vehicle frame) and $\psi, \dot{\psi}$ are the heading angle and yaw rate, respectively, and V_{x_KP}, V_{y_KP} are the longitudinal and lateral velocities, respectively (vehicle frame).

Then, the velocities in the vehicle frame are expressed as

$$\begin{aligned} \dot{V}_{x_KP} &= a_{x_KP} + V_{y_KP} \cdot \dot{\psi}, \\ \dot{V}_{y_KP} &= a_{y_KP} - V_{x_KP} \cdot \dot{\psi}. \end{aligned} \quad (9)$$

$$\begin{bmatrix} V_{x_KP}(k) \\ V_{y_KP}(k) \\ \psi(k) \end{bmatrix} = \begin{bmatrix} V_{x_KP}(k-1) + \Delta T \cdot a_{x_KP}(k-1) + \Delta T \cdot V_{y_KP}(k-1) \cdot \dot{\psi}(k-1) + \eta_{V_{x_KP}} \\ V_{y_KP}(k-1) + \Delta T \cdot a_{y_KP}(k-1) - \Delta T \cdot V_{x_KP}(k-1) \cdot \dot{\psi}(k-1) + \eta_{V_{y_KP}} \\ \psi(k-1) + \Delta T \cdot \dot{\psi}(k-1) + \eta_{\psi} \end{bmatrix}, \quad (11)$$

where $\eta_{V_{x_KP}}, \eta_{V_{y_KP}},$ and η_{ψ} are white noise in the longitudinal/lateral velocities and in the heading angle, respectively.

2.2.4. Measurement Equations for the Implemented Filter (i-EKF). In order to define the best cost-benefit layout of the proposed measurement system, different sensor configurations are considered in this study (Figure 4). Three low-cost GPS receivers, denoted as GPS_1, GPS_2, and GPS_KP, are considered, as shown in Figure 4.

The readings acquired from each of the receivers are the speed and path angle of each of the points at which the receivers are located.

GPS_1: V_{GPS_1}, v_1 , coordinates (x_1, y_1) in the vehicle frame

GPS_2: V_{GPS_2}, v_2 , coordinates (x_2, y_2) in the vehicle frame

GPS_KP: V_{GPS_KP}, v_{KP} , coordinates $(x_{KP}, y_{KP}) = (0, 0)$ in the vehicle frame

The measured speed for each GPS receiver is considered to represent the horizontal velocity (E, N) of each point.

The speed of each of the points in the reference frame (E, N) can be expressed in terms of the GPS measurement (Figure 5). For instance, the speed of point 1 can be expressed as

$$\begin{aligned} V_{E.1} &= V_{GPS.1} \cdot \cos v_1, \\ V_{N.1} &= V_{GPS.1} \cdot \sin v_1. \end{aligned} \quad (12)$$

In discrete form, they can be expressed as

$$\begin{aligned} \dot{V}_{x_KP} &\approx \frac{V_{x_KP}(k) - V_{x_KP}(k-1)}{\Delta T} \\ &= a_{x_KP}(k-1) + V_{y_KP}(k-1) \cdot \dot{\psi}(k-1), \\ \dot{V}_{y_KP} &\approx \frac{V_{y_KP}(k) - V_{y_KP}(k-1)}{\Delta T} \\ &= a_{y_KP}(k-1) - V_{x_KP}(k-1) \cdot \dot{\psi}(k-1), \\ \dot{\psi} &\approx \frac{\psi(k) - \psi(k-1)}{\Delta T} = \dot{\psi}(k-1). \end{aligned} \quad (10)$$

However, in the simplified model, these inaccuracies are included in noise system. The model can be expressed in matrix form as

Furthermore, the speed of a point of the semitrailer can be expressed in terms of the speed of another point (e.g., the kingpin). The velocity of point 1 in the vehicle frame is expressed as

$$\begin{aligned} V_{x.1} &= V_{x_KP} - y_1 \dot{\psi}, \\ V_{y.1} &= V_{y_KP} + x_1 \dot{\psi}. \end{aligned} \quad (13)$$

The velocity of point 1 in the reference frame can be expressed as

$$\begin{aligned} V_{E.1} &= V_{x.1} \cdot \cos \psi - V_{y.1} \cdot \sin \psi, \\ V_{N.1} &= V_{x.1} \cdot \sin \psi + V_{y.1} \cdot \cos \psi. \end{aligned} \quad (14)$$

The GPS planar velocities (east/north velocities of any GPS antenna) can be expressed as functions of the longitudinal/lateral velocities, yaw rate, and heading angle as follows:

$$\begin{aligned} V_{E.1} &= V_{GPS.1} \cdot \cos v_1 \\ &= (V_{x_KP} - y_1 \dot{\psi}) \cdot \cos \psi \\ &\quad - (V_{y_KP} + x_1 \dot{\psi}) \cdot \sin \psi, \\ V_{N.1} &= V_{GPS.1} \cdot \sin v_1 \\ &= (V_{x_KP} - y_1 \dot{\psi}) \cdot \sin \psi \\ &\quad + (V_{y_KP} + x_1 \dot{\psi}) \cdot \cos \psi, \end{aligned}$$

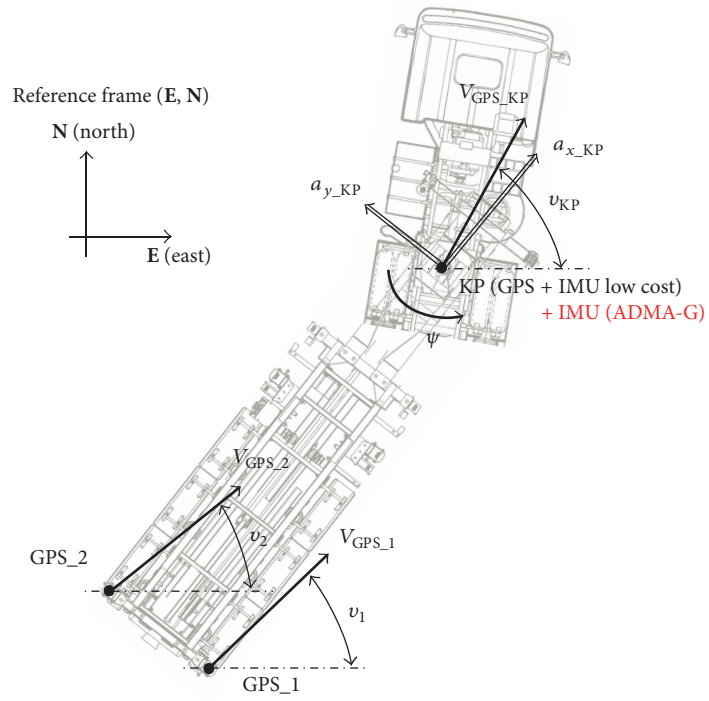


FIGURE 4: Sensors configurations for the proposed measurements system.

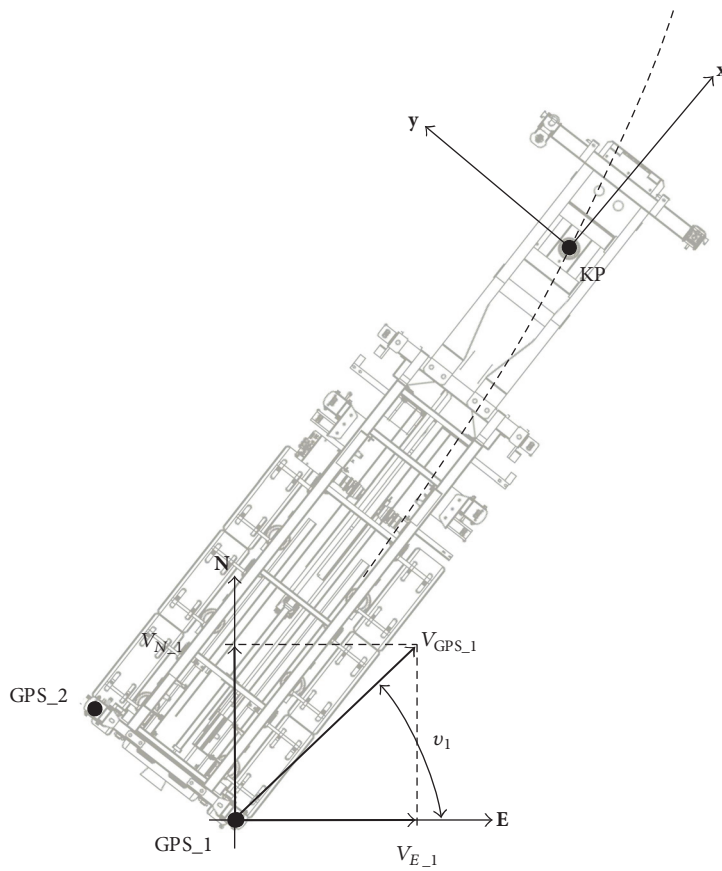


FIGURE 5: GPS speed in reference frame.

$$\begin{aligned}
V_{E,2} &= V_{\text{GPS},2} \cdot \cos v_2 \\
&= (V_{x,\text{KP}} - y_2 \dot{\psi}) \cdot \cos \psi \\
&\quad - (V_{y,\text{KP}} + x_2 \dot{\psi}) \cdot \sin \psi, \\
V_{N,2} &= V_{\text{GPS},2} \cdot \sin v_2 = (V_{x,\text{KP}} - y_2 \dot{\psi}) \cdot \sin \psi \\
&\quad + (V_{y,\text{KP}} + x_2 \dot{\psi}) \cdot \cos \psi, \\
V_{E,\text{KP}} &= V_{\text{GPS},\text{KP}} \cdot \cos v_{\text{KP}} \\
&= V_{x,\text{KP}} \cdot \cos \psi - V_{y,\text{KP}} \cdot \sin \psi, \\
V_{N,\text{KP}} &= V_{\text{GPS},\text{KP}} \cdot \sin v_{\text{KP}} \\
&= V_{x,\text{KP}} \cdot \sin \psi + V_{y,\text{KP}} \cdot \cos \psi.
\end{aligned} \tag{15}$$

2.2.5. Implementation of *i*-EKF. For estimation of a system/process with nonlinear difference and measurement relationships, the linearisation and estimation equations are rewritten as

$$\begin{aligned}
x(k) &\approx \tilde{x}(k) + \mathbf{F}(x(k-1) - \hat{x}(k-1)) \\
&\quad + \mathbf{W}w(k-1), \\
y(k) &\approx \tilde{y}(k) + \mathbf{H}(x(k) - \tilde{x}(k)) + \mathbf{V}v(k),
\end{aligned} \tag{16}$$

where $x(k)$ and $y(k)$ are the actual state and measurement vectors, respectively; $\tilde{x}(k)$ and $\tilde{y}(k)$ are the approximate state and measurement vectors, respectively; $\hat{x}(k)$ is an *a posteriori* estimate of the state at step k ; \mathbf{F} is the Jacobian matrix of partial derivatives of \mathbf{f} with respect to x ; that is,

$$F_{[i,j]} = \frac{\partial f_{[i]}}{\partial x_{[j]}}(\hat{x}(k-1), u(k-1), 0); \tag{17}$$

\mathbf{W} is the Jacobian matrix of partial derivatives of \mathbf{f} with respect to w ; that is,

$$W_{[i,j]} = \frac{\partial f_{[i]}}{\partial w_{[j]}}(\hat{x}(k-1), u(k-1), 0); \tag{18}$$

\mathbf{H} is the Jacobian matrix of partial derivatives of \mathbf{h} with respect to x ; that is,

$$H_{[i,j]} = \frac{\partial h_{[i]}}{\partial x_{[j]}}(\tilde{x}(k), 0); \tag{19}$$

\mathbf{V} is the Jacobian matrix of partial derivatives of \mathbf{h} with respect to v ; that is,

$$V_{[i,j]} = \frac{\partial h_{[i]}}{\partial v_{[j]}}(\tilde{x}(k), 0). \tag{20}$$

Note that, for simplicity of notation, the time-step subscript k is not attached to the Jacobians \mathbf{F} , \mathbf{W} , \mathbf{H} , and \mathbf{V} , despite the fact that they are different at each time step.

i-EKF *Time Update Equations.* The complete set of EKF equations is shown below. Note that we have substituted $\tilde{x}^- (k)$ for $\tilde{x}(k)$ to ensure consistency with the earlier “super minus” *a priori* notation and that we now attach the time-step subscript to the Jacobians \mathbf{F} , \mathbf{W} , \mathbf{H} , and \mathbf{V} to reinforce the notion that they are different at (and therefore must be recomputed at) each time step. The time update equations project the state and covariance estimates from the previous time step $k-1$ to the current time step k . \mathbf{F}_k and \mathbf{W}_k are the process Jacobians at step k , and \mathbf{Q}_k is the process noise covariance at step k .

$$\tilde{x}^-(k) = \mathbf{f}(\hat{x}(k-1), u(k-1), 0), \tag{21}$$

$$\mathbf{P}_k^- = \mathbf{F}_k \mathbf{P}_{k-1} \mathbf{F}_k^T + \mathbf{W}_k \mathbf{Q}_{k-1} \mathbf{W}_k^T.$$

i-EKF *Measurement Update Equations.* The measurement update equations correct the state and covariance estimates using the measurement $y(k)$. \mathbf{H}_k and \mathbf{V} are the measurement Jacobians at step k , and \mathbf{R}_k is the measurement noise covariance at step k . (Note that we now attach the subscript to the Jacobians, thereby permitting their change with each measurement.)

$$\mathbf{K}_k = \mathbf{P}_k^- \mathbf{H}_k^T (\mathbf{H}_k \mathbf{P}_k^- \mathbf{H}_k^T + \mathbf{R}_k)^{-1},$$

$$\hat{x}(k) = \tilde{x}^-(k) + \mathbf{K}_k (y(k) - h(\tilde{x}^-(k), 0)), \tag{22}$$

$$\mathbf{P}_k = (\mathbf{I} - \mathbf{K}_k \mathbf{H}_k) \mathbf{P}_k^-.$$

\mathbf{f} can be expressed in matrix form as follows:

$$\mathbf{f} = \begin{bmatrix} f_1(k) \\ f_2(k) \\ f_3(k) \end{bmatrix} = \begin{bmatrix} V_{x,\text{KP}}(k-1) + \Delta T \cdot a_{x,\text{KP}}(k-1) + \Delta T \cdot V_{y,\text{KP}}(k-1) \cdot \dot{\psi}(k-1) + \eta_{V_{x,\text{KP}}} \\ V_{y,\text{KP}}(k-1) + \Delta T \cdot a_{y,\text{KP}}(k-1) - \Delta T \cdot V_{x,\text{KP}}(k-1) \cdot \dot{\psi}(k-1) + \eta_{V_{y,\text{KP}}} \\ \psi(k-1) + \Delta T \cdot \dot{\psi}(k-1) + \eta_{\psi} \end{bmatrix}. \tag{23}$$

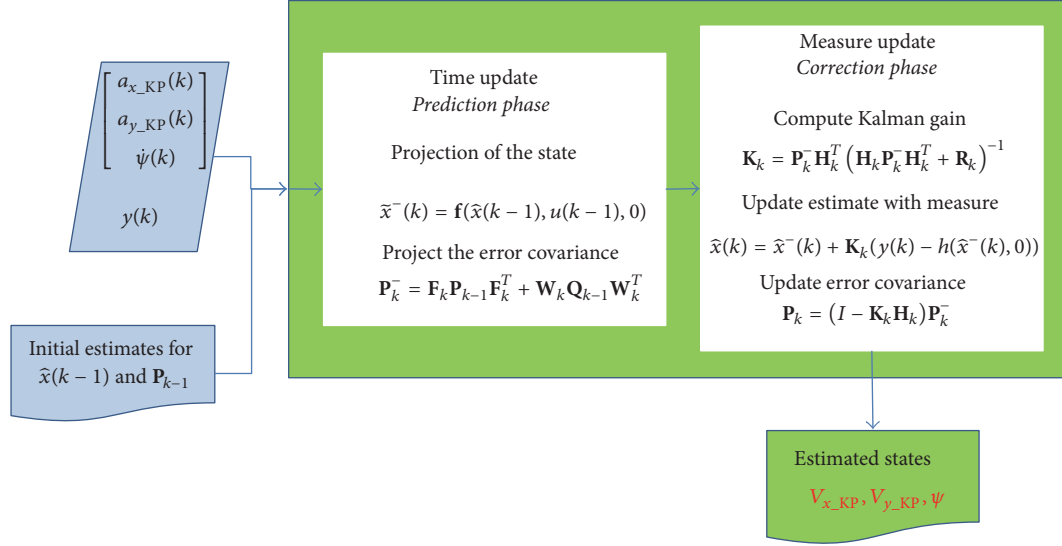


FIGURE 6: i-EKF for vehicle kinematics estimation.

The matrices \mathbf{F} and \mathbf{W} are, respectively, given as

$$\mathbf{F} = \begin{bmatrix} \frac{\partial f_1}{\partial V_{x_KP}} & \frac{\partial f_1}{\partial V_{y_KP}} & \frac{\partial f_1}{\partial \psi} \\ \frac{\partial f_2}{\partial V_{x_KP}} & \frac{\partial f_2}{\partial V_{y_KP}} & \frac{\partial f_2}{\partial \psi} \\ \frac{\partial f_3}{\partial V_{x_KP}} & \frac{\partial f_3}{\partial V_{y_KP}} & \frac{\partial f_3}{\partial \psi} \end{bmatrix}$$

$$= \begin{bmatrix} 1 & \Delta T \cdot \dot{\psi}(k) & 0 \\ -\Delta T \cdot \dot{\psi}(k) & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}, \quad (24)$$

$$\mathbf{W} = \begin{bmatrix} \frac{\partial f_1}{\partial \eta_{V_{x_KP}}} & \frac{\partial f_1}{\partial \eta_{V_{y_KP}}} & \frac{\partial f_1}{\partial \eta_{\psi}} \\ \frac{\partial f_2}{\partial \eta_{V_{x_KP}}} & \frac{\partial f_2}{\partial \eta_{V_{y_KP}}} & \frac{\partial f_2}{\partial \eta_{\psi}} \\ \frac{\partial f_3}{\partial \eta_{V_{x_KP}}} & \frac{\partial f_3}{\partial \eta_{V_{y_KP}}} & \frac{\partial f_3}{\partial \eta_{\psi}} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}.$$

Table 1 presents the study cases corresponding to the different sensor configurations analysed in this study.

The measurement vector $y(k)$ and the related \mathbf{h} matrix for the study cases described in Table 1 are presented in Table 2.

The complete set of i-EKF equations is shown in Figure 6.

2.2.6. Sensors and Covariance Matrices. In practice, the matrices of the *process noise covariance* \mathbf{Q} and *measurement noise covariance* \mathbf{R} may change with each time step or

TABLE 1: Study cases corresponding to different sensor configurations.

Case	Input		Measurement		Reference	
	IMU	KP	GPS_1	GPS_2	GPS_KP	ADMA_KP REF
0	×					×
1	×				V_{E_KP}, V_{N_KP}	×
2	×		V_{E_1}, V_{N_1}			×
3	×		V_{E_1}, V_{N_1}	V_{E_2}, V_{N_2}		×
4	×		V_{E_1}, V_{N_1}	V_{E_2}, V_{N_2}	V_{E_KP}, V_{N_KP}	×

measurement. However, they can be assumed as constant. The matrix \mathbf{Q} can be expressed as

$$E[w(k)w(k)^T] = \mathbf{Q},$$

$$\mathbf{Q} = \begin{bmatrix} \sigma_{\eta_{V_{x_KP}}}^2 & \sigma_{\eta_{V_{x_KP}}\eta_{V_{y_KP}}} & \sigma_{\eta_{V_{x_KP}}\eta_{\psi}} \\ \sigma_{\eta_{V_{x_KP}}\eta_{V_{y_KP}}} & \sigma_{\eta_{V_{y_KP}}}^2 & \sigma_{\eta_{V_{y_KP}}\eta_{\psi}} \\ \sigma_{\eta_{V_{x_KP}}\eta_{\psi}} & \sigma_{\eta_{V_{y_KP}}\eta_{\psi}} & \sigma_{\eta_{\psi}}^2 \end{bmatrix}. \quad (25)$$

If the errors are considered as being independent, the covariance can be neglected; that is,

$$\sigma_{\eta_{V_{x_KP}}\eta_{V_{y_KP}}} = \sigma_{\eta_{V_{x_KP}}\eta_{\psi}} = \sigma_{\eta_{V_{y_KP}}\eta_{\psi}} = 0. \quad (26)$$

For characterisation of the vehicle's dynamics, it is instrumented using a low-cost IMU at the point of its coupling with the truck, which is the kingpin (indicated as "KP" in Figure 3). The following readings acquired from the IMU

TABLE 2: Measurement vector (y) and related \mathbf{h} matrix for the considered study cases.

Case	y	\mathbf{h}
0	No GPS signal Integration of acceleration signals acquired from IMU	—
1	$\begin{pmatrix} V_{E,KP} \\ V_{N,KP} \end{pmatrix}$	$\begin{pmatrix} V_{x,KP} \cdot \cos \psi - V_{y,KP} \cdot \sin \psi \\ V_{x,KP} \cdot \sin \psi + V_{y,KP} \cdot \cos \psi \end{pmatrix}$
2	$\begin{pmatrix} V_{E,1} \\ V_{N,1} \end{pmatrix}$	$\begin{pmatrix} (V_{x,KP} - y_1 \dot{\psi}) \cdot \cos \psi - (V_{y,KP} + x_1 \dot{\psi}) \cdot \sin \psi \\ (V_{x,KP} - y_1 \dot{\psi}) \cdot \sin \psi + (V_{y,KP} + x_1 \dot{\psi}) \cdot \cos \psi \end{pmatrix}$
3	$\begin{pmatrix} V_{E,1} \\ V_{N,1} \\ V_{E,2} \\ V_{N,2} \end{pmatrix}$	$\begin{pmatrix} (V_{x,KP} - y_1 \dot{\psi}) \cdot \cos \psi - (V_{y,KP} + x_1 \dot{\psi}) \cdot \sin \psi \\ (V_{x,KP} - y_1 \dot{\psi}) \cdot \sin \psi + (V_{y,KP} + x_1 \dot{\psi}) \cdot \cos \psi \\ (V_{x,KP} - y_2 \dot{\psi}) \cdot \cos \psi - (V_{y,KP} + x_2 \dot{\psi}) \cdot \sin \psi \\ (V_{x,KP} - y_2 \dot{\psi}) \cdot \sin \psi + (V_{y,KP} + x_2 \dot{\psi}) \cdot \cos \psi \end{pmatrix}$
4	$\begin{pmatrix} V_{E,1} \\ V_{N,1} \\ V_{E,2} \\ V_{N,2} \\ V_{E,KP} \\ V_{N,KP} \end{pmatrix}$	$\begin{pmatrix} (V_{x,KP} - y_1 \dot{\psi}) \cdot \cos \psi - (V_{y,KP} + x_1 \dot{\psi}) \cdot \sin \psi \\ (V_{x,KP} - y_1 \dot{\psi}) \cdot \sin \psi + (V_{y,KP} + x_1 \dot{\psi}) \cdot \cos \psi \\ (V_{x,KP} - y_2 \dot{\psi}) \cdot \cos \psi - (V_{y,KP} + x_2 \dot{\psi}) \cdot \sin \psi \\ (V_{x,KP} - y_2 \dot{\psi}) \cdot \sin \psi + (V_{y,KP} + x_2 \dot{\psi}) \cdot \cos \psi \\ V_{x,KP} \cdot \cos \psi - V_{y,KP} \cdot \sin \psi \\ V_{x,KP} \cdot \sin \psi + V_{y,KP} \cdot \cos \psi \end{pmatrix}$

(which includes three accelerometers and three gyroscopes) are considered:

$a_{x,KP}^{\text{accel}}$: longitudinal acceleration, vehicle frame

$a_{y,KP}^{\text{accel}}$: lateral acceleration, vehicle frame

r^{gyro} : yaw rate

If the effect of gravity is neglected and the movement plane is considered (while neglecting the effects of pitch and roll), the following expressions allow relating the dynamic behaviour of the vehicle with the IMU measurement at the KP:

$$\begin{aligned}
 a_{x,KP}^{\text{accel}} &= \dot{V}_{x,KP} - V_{y,KP} \cdot \dot{\psi} + b_{a_x} + \eta_{a_x}, \\
 a_{y,KP}^{\text{accel}} &= \dot{V}_{y,KP} + V_{x,KP} \cdot \dot{\psi} + b_{a_y} + \eta_{a_y}, \\
 r^{\text{gyro}} &= \dot{\psi} + b_{\text{gyro}} + \eta_r,
 \end{aligned} \tag{27}$$

where b_{a_x} , b_{a_y} , and b_{gyro} are the biases of the longitudinal/lateral accelerometer and rate gyro, respectively, and η_{a_x} , η_{a_y} , and η_r are white noise in the longitudinal/lateral accelerometer and that in the rate gyro, respectively.

The three bias terms (b_{a_x} , b_{a_y} , and b_{gyro}) of the IMU measurements are assumed to be constant throughout the

TABLE 3: Statistical characterisation of sensors and dispersion of measurements as obtained from the experimental program.

Sensor	Obtained error properties
IMU	$N(0, \sigma_{a_x^{\text{IMU}}}) = N(0, 1.8320e - 06) \text{ m/s}^2$
	$N(0, \sigma_{a_y^{\text{IMU}}}) = N(0, 6.5881e - 07) \text{ m/s}^2$
GPS	$N(0, \sigma_{r^{\text{IMU}}}) = N(0, 0.0085) \text{ rad/s}$
	Standard deviation of white noise $N(0, \sigma_{V_{\text{GPS}}}) = N(0, 0.03) \text{ m/s}$

measurement windows [46]. To evaluate this case, the following can be considered:

$$\begin{aligned}
 \sigma_{\eta_{V_{x,KP}}} &= \Delta T \cdot \sigma_{a_{x,KP}^{\text{IMU}}}; \\
 \sigma_{\eta_{V_{y,KP}}} &= \Delta T \cdot \sigma_{a_{y,KP}^{\text{IMU}}}; \\
 \sigma_{\eta_{\psi}} &= \Delta T \cdot \sigma_{r^{\text{IMU}}},
 \end{aligned} \tag{28}$$

where the matrix \mathbf{Q} can also be expressed as follows:

$$\mathbf{Q} = (\Delta T)^2 \cdot \begin{pmatrix} \sigma_{a_{x,KP}^{\text{IMU}}}^2 & \sigma_{a_{x,KP}^{\text{IMU}}} \sigma_{a_{y,KP}^{\text{IMU}}} & \sigma_{a_{x,KP}^{\text{IMU}}} \sigma_{r^{\text{IMU}}} \\ \sigma_{a_{x,KP}^{\text{IMU}}} \sigma_{a_{y,KP}^{\text{IMU}}} & \sigma_{a_{y,KP}^{\text{IMU}}}^2 & \sigma_{a_{y,KP}^{\text{IMU}}} \sigma_{r^{\text{IMU}}} \\ \sigma_{a_{x,KP}^{\text{IMU}}} \sigma_{r^{\text{IMU}}} & \sigma_{a_{y,KP}^{\text{IMU}}} \sigma_{r^{\text{IMU}}} & \sigma_{r^{\text{IMU}}}^2 \end{pmatrix}. \tag{29}$$

The obtained dispersion of measurements and the statistical characterisation of the low-cost IMU and GPS receivers after completion of the virtual experimental program are as presented in Table 3.



FIGURE 7: (a) Low-cost IMU [6]; (b) GPS VBOX Sport [7]; (c) vehicle sensing with high-accuracy IMU (ADMA-G-EntryLevel, GeneSys) of the validation system.

The measurement noise covariance \mathbf{R} is a diagonal matrix because all measurements are independent of each other and their size is dependent on the analysed measures, according to the study cases presented in Table 1.

$$\mathbf{R} = \begin{pmatrix} \sigma_{z_1}^2 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \sigma_{z_n}^2 \end{pmatrix} = \begin{pmatrix} 0.03 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & 0.03 \end{pmatrix}. \quad (30)$$

3. Results of the Implementation in Real Vehicle

For application of the proposed instrumentation system to a real vehicle and for analysing the best cost-benefit layout, an experimental test program was developed. To this end, a semitrailer was equipped with sensors required to apply the proposed methodology and to validate its results. Details of this test program are as follows:

- (i) The developed measurement system included a low-cost IMU (Figure 7(a)) and three GPS receivers (Figure 7(b)). The chosen low-cost IMU was the UM7-LT orientation sensor of CH Robotics [6], and the GPS receiver was VBOX Sport by Racelogic [7].
- (ii) The validation system was composed of a high-accuracy IMU (ADMA-G-EntryLevel, GeneSys, [47]), as shown in Figure 7(c).

In order to perform the validation, the relative errors of the velocities (longitudinal and lateral) estimated in the vehicle frame were calculated using the following expressions:

$$eV_{x_{relk}} = \frac{|V_{x_{IMU_{ADMA,G}}} - V_{x_{estimated}}|}{\max(V_{x_{IMU_{ADMA,G}})}, \quad (31)$$

$$eV_{y_{relk}} = \frac{|V_{y_{IMU_{ADMA,G}}} - V_{y_{estimated}}|}{\max(V_{y_{IMU_{ADMA,G}})},$$



FIGURE 8: Example of trajectory of instrumented vehicle in experimental test program.

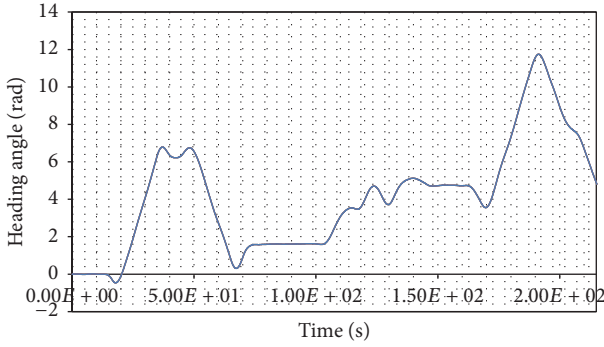


FIGURE 9: Heading angle versus time of instrumented vehicle in experimental test program.

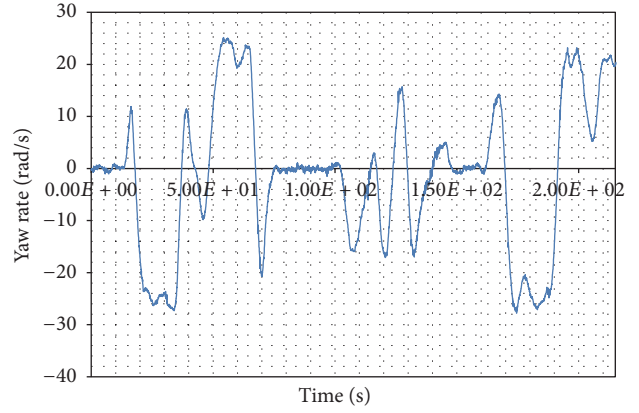


FIGURE 10: Yaw rate versus time of instrumented vehicle in experimental test program.

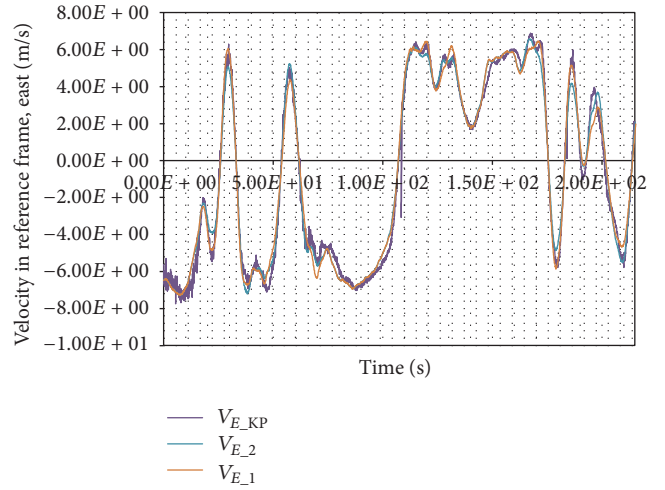


FIGURE 11: Velocities in reference frame (east coordinate) versus time from GPS receivers in experimental test program.

TABLE 4: Maximum errors for different sensor configurations.

Case	$\max(eV_{x_{rel,k}})$	$\max(eV_{y_{rel,k}})$
0: IMU KP only	0.020	0.0069
1: IMU KP + GPS_KP	0.0051	0.0029
2: IMU KP + GPS_1	0.0095	0.002883
3: IMU KP + GPS_1 + GPS_2	0.0135	0.00183
4: IMU KP + GPS_1 + GPS_2 + GPS_KP	0.000508	0.00165

where $eV_{x_{rel,k}}$ and $eV_{y_{rel,k}}$ are the relative errors of the longitudinal and lateral velocities, respectively, estimated in the vehicle frame in step k . The manoeuvre shown in Figure 8 was performed using the instrumented vehicle. Then, following the completion of the experiment, the errors for the different sensor configurations considered were calculated. In Figures 9–13, different plots of measured variables are shown.

The plots of relative errors (longitudinal and lateral) are shown in Figures 14 and 15 and maximum values of errors for the different sensor configurations are presented in Table 4.

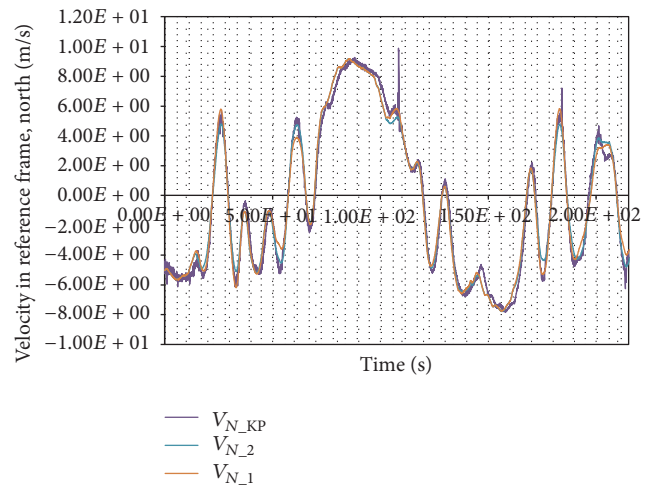


FIGURE 12: Velocities in reference frame (north coordinate) versus time from GPS receivers in experimental test program.

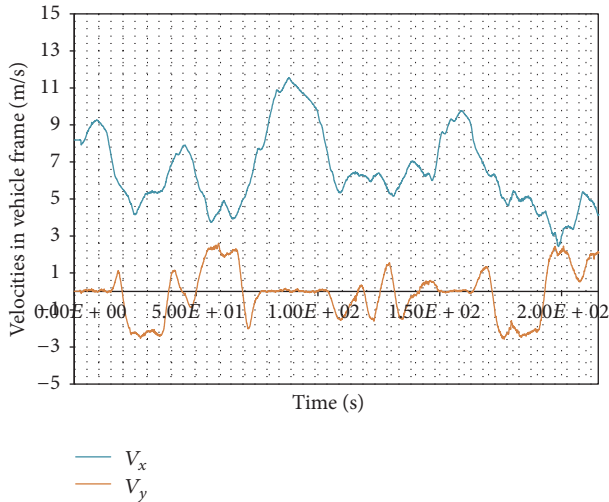


FIGURE 13: Velocities in vehicle frame (x: longitudinal; y: lateral) versus time of instrumented vehicle in experimental test program.

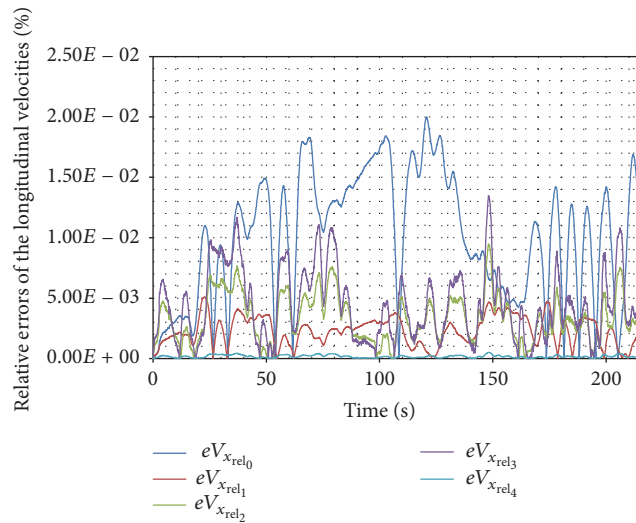


FIGURE 14: Plot of relative errors of the longitudinal velocities in the proposed cases.

4. Conclusions and Future Work

Study of the fatigue life of freight vehicles in general and of semitrailers in particular requires knowledge of the loads to which they are subjected. In the present study, dynamics simulations were developed for this purpose, in which the inputs of these simulations were the kinematic variables of the kingpin. In order to determine the states of loads to which a fleet of vehicles is subjected, a vehicle-mountable low-cost instrumentation system was developed, which can be used in real movement conditions with acceptable accuracy.

This flexible instrumentation system includes a combination of sensors, that is, an IMU and GPS antennas, as well as a software-based extended Kalman filter for estimations in consideration of system nonlinearities.

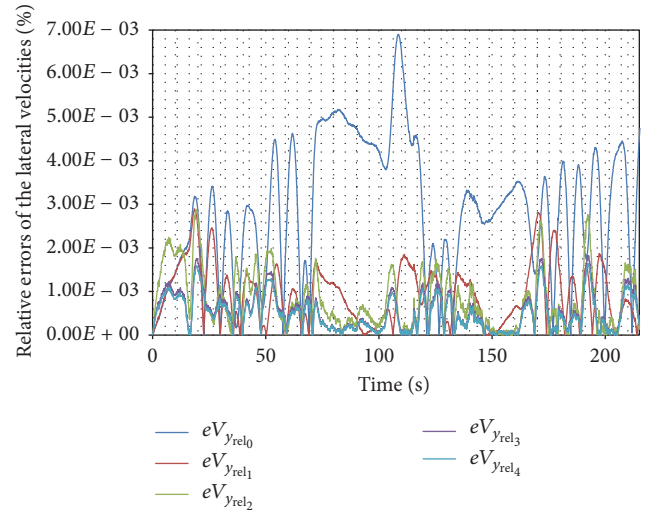


FIGURE 15: Plot of relative errors of the lateral velocities in the proposed cases.

Various sensor configurations were proposed to enhance the estimation accuracy of the proposed system, and the best sensor configuration was found to be the one corresponding to Case 4 in Table 4.

Future work includes implementation of the developed instrumentation system in a fleet of vehicles in collaboration with a semitrailer manufacturer, with the aim of characterising the loads in service and estimating the vehicle fatigue life as the basis for process redesign and structural optimisation.

Competing Interests

The authors declare no competing interests.

Authors' Contributions

Pablo Luque, Daniel A. Mántaras, and Aida Rodríguez conceived and designed the main localisation scheme and formulated the mathematical model. Javier G. Jalón and José L. López performed analysis of the IMU errors and collaborated for establishment of the mathematical model. Finally, Ángel Martín, Luis Castejón, Hugo Malón, and Marco Carrera designed and performed the experiments and validated the experimental results.

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Carrera Alegre, Principal Investigator of different projects concerning this topic, who unexpectedly died last May 20 (may he rest in peace).

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